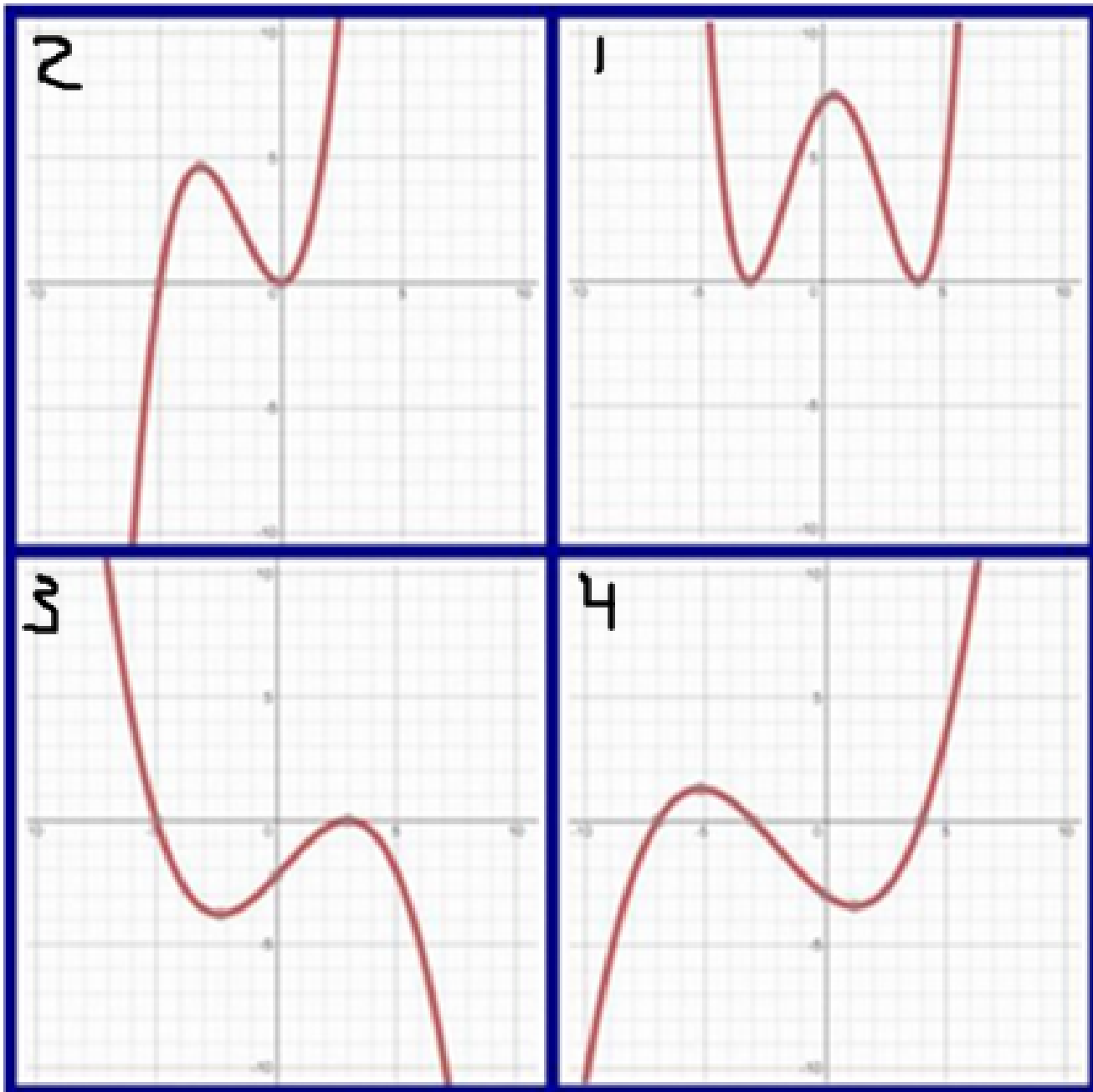


Which one doesn't belong?



$$f(x) = 4 - 3x^2 - x^3$$

$$f(x) = -x^3 - 3x^2 + 4$$

• degree 3

• $a < 0$

Start high
end low

• y int ($x=0$)
(0, 4)

• x int ($y=0$)

$$0 = -x^3 - 3x^2 + 4$$

$$0 = -(x^3 + 3x^2 - 4)$$

RRT $P(x) = x^3 + 3x^2 - 4$

$$a = \pm 1 \quad b = \pm 1, \pm 2, \pm 4$$

$$P\left(\frac{b}{a}\right) = 0 \quad P(1) = 1 + 3 - 4 = 0$$

$$\begin{array}{r|rrrr} 1 & 1 & 3 & 0 & -4 \\ & \downarrow & 1 & 4 & 4 \\ \hline & 1 & 4 & 4 & 0 \end{array}$$

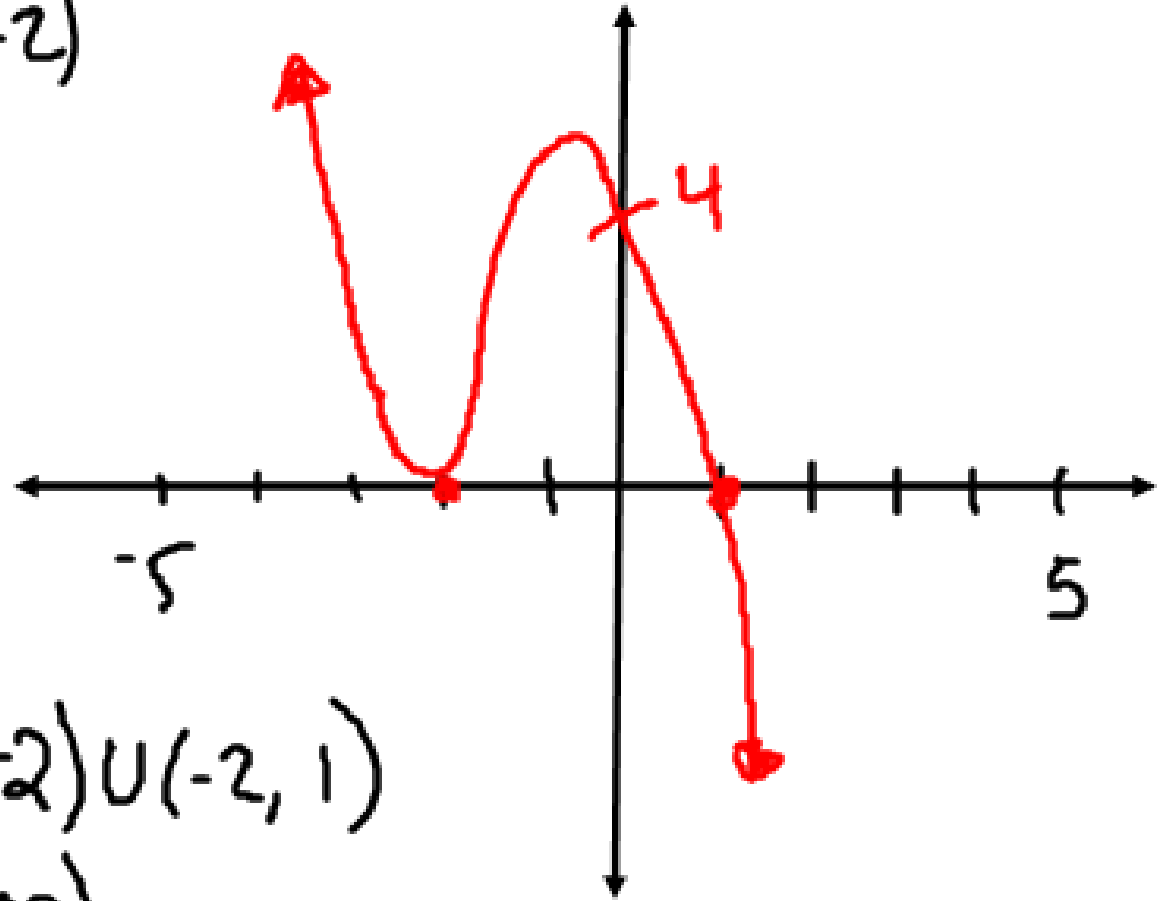
$$P(x) = (x-1)(x^2+4x+4) \\ = (x-1)(x+2)(x+2)$$

$$0 = -(x-1)(x+2)(x+2)$$

x int:

(1, 0) (-2, 0)

↑
Bounce



$$f(x) > 0 : x \in (-\infty, -2) \cup (-2, 1)$$

$$f(x) < 0 : x \in (1, +\infty)$$

$$f(x) = -x^{(4)} + 4x^3 - x^2 - 6x$$

$$f(x) = -x(x^3 - 4x^2 + x + 6) \rightarrow f(x) = -x^{(x-6)}(x-2)(x-3)(x+1)$$

$$P(x) = 1x^3 - 4x^2 + x + 6$$

$$a = \pm 1$$

$$b = \pm 1, \pm 2, \pm 3, \pm 6$$

$$\frac{b}{a} = \pm 1, \pm 2, \pm 3, \pm 6$$

$$P(2) = 8 - 16 + 2 + 6 = 0$$

$$\begin{array}{r|rrrr} 2 & 1 & -4 & 1 & 6 \\ & \downarrow & 2 & -4 & -6 \\ \hline & 1 & -2 & -3 & 0 \end{array}$$

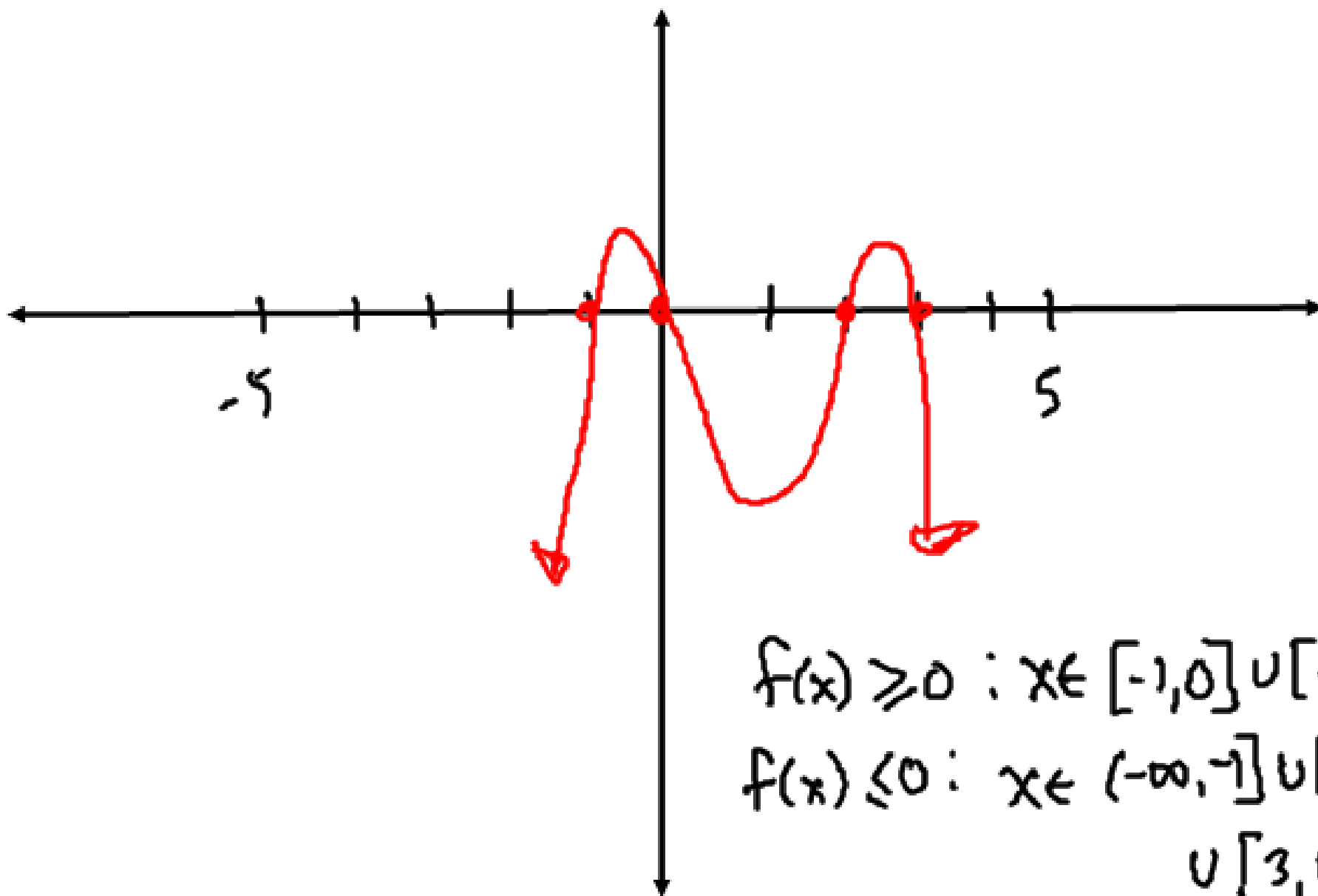
$$P(x) = (x-2)(x^2 - 2x - 3) \\ = (x-2)(x-3)(x+1)$$

• degree: 4

• end behaviour: Start low end low

• y-int ($x=0$)
(0,0)

• x-int ($y=0$)
(2,0) (3,0) (-1,0) (0,0)

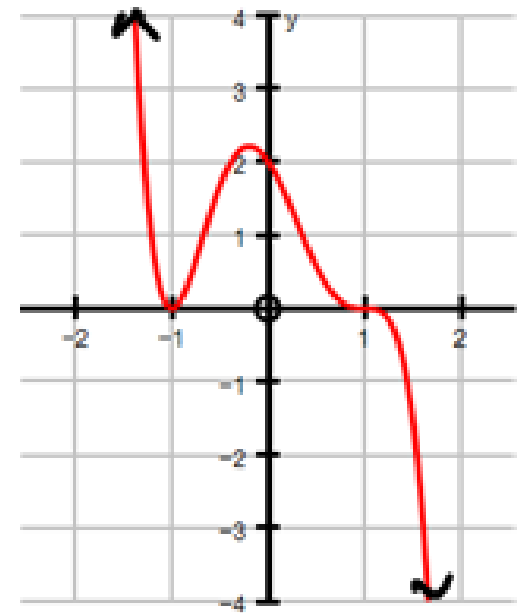


$$f(x) \geq 0 : x \in [-1, 0] \cup [2, 3]$$

$$f(x) \leq 0 : x \in (-\infty, -1] \cup [0, 2] \cup [3, \infty)$$

For the polynomial graphed below, determine:

- the sign of the leading coefficient
- the x and y -intercepts
- the intervals where the function is positive and the intervals where it is negative
- the equation for the polynomial function (in factored and expanded form)



a) $a < 0$

b) y -int $(0, 2)$

x -int $(-1, 0)$ $(1, 0)$

c) $f(x) > 0: x \in (-\infty, -1) \cup (-1, 1)$

$f(x) < 0: x \in (1, \infty)$

d) $0 = (x+1)^2 (x-1)^3$

$y = a(x+1)^2 (x-1)^3$

$2 = a(0+1)^2(0-1)^3$

$2 = -a$

$-2 = a$

$y = -2(x+1)^2(x-1)^3 \leftarrow$ factored form.

$$y = -2(x+1)^2(x-1)^3$$

$$= -2(x+1)(x+1)(x-1)(x-1)(x-1)$$

$$= -2(x+1)(x-1)(x+1)(x-1)(x-1)$$

$$= -2(x^2-1)(x^2-1)(x-1)$$

$$= -2(x^4 - 2x^2 + 1)(x-1)$$

$$= -2(x^5 - x^4 - 2x^3 + 2x^2 + x - 1)$$

$$= -2x^5 + 2x^4 + 4x^3 - 4x^2 - 2x + 2 \leftarrow \text{expanded form.}$$

Your Turn

Three consecutive integers have a product of -210 .

- Write a polynomial function to model this situation.
- What are the three integers?

let a number be n

$$-210 = (n-1)(n)(n+1)$$

$$-210 = (n^2 - 1)(n)$$

$$-210 = n^3 - n$$

$$0 = n^3 - n + 210$$

← one after another
← I whole

← multiply

$$(n-1)(n)(n+1)$$

$$(n-2)(n-1)(n)$$

$$(n)(n+1)(n+2)$$

RRT $P(n) = n^3 - n + 210$

$$a = \pm 1 \quad b = \pm 1, \pm 2, \pm 3, \pm 5, \pm 6, \pm 7$$

$$\frac{a}{b} =$$

$$P(-6) = 0$$

$$\begin{array}{r|rrrr} -6 & 1 & 0 & -1 & 210 \\ & & \downarrow -6 & 36 & -210 \\ \hline & 1 & -6 & 35 & 0 \end{array}$$

$$P(n) = (n+6)(n^2 - 6n + 35)$$

Discriminant $\Delta = b^2 - 4ac$

- $\Delta < 0$

$P(n) = (n+6)(n^2 - 6n + 35)$

no real roots

$0 = (n+6)(n^2 - 6n + 35)$

$n+6=0$

$n=-6$

our 1st # is -7
2nd # is -6
3rd # is -5

Your Turn

Three consecutive integers have a product of -210 .

- Write a polynomial function to model this situation.
- What are the three integers?

let a number be n

$$-210 = n(n+1)(n+2)$$

$$-210 = (n^2+n)(n+2)$$

$$-210 = n^3 + 2n^2 + n^2 + 2n$$

$$0 = n^3 + 3n^2 + 2n + 210$$

↓ order
↓ of whole
to 5

↓ multiply

$$\left(\begin{array}{l} (n)(n-1)(n-2) \\ (n-1)(n)(n+1) \end{array} \right)$$

$$a: \pm 1 \quad b: \pm 1, \pm 2, \pm 3, \pm 5, \pm 7, \pm 10$$

$$P(n) = n^3 + 3n^2 + 2n + 210$$

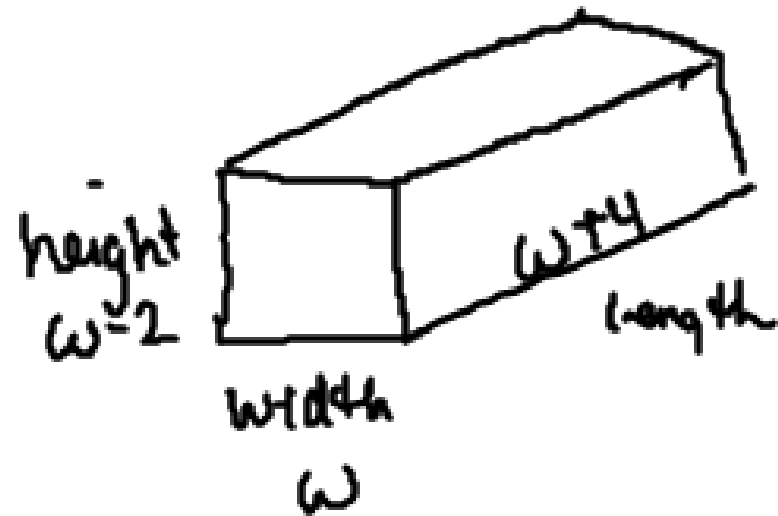
$$P(-7) = 0$$

-7	1	3	2	210
	↓	-7	28	-210
	1	-4	30	

$$P(n) = (n+7)(n^2 - 4n + 30)$$

Discriminant $\Delta = b^2 - 4ac$
 $\Delta < 0$

15. The width of a rectangular prism is w centimetres. The height is 2 cm less than the width. The length is 4 cm more than the width. If the magnitude of the volume of the prism is 8 times the measure of the length, what are the dimensions of the prism?



$$V = l \times w \times h$$

$$= (w+4)(w)(w-2)$$

$$8(w+4) = (w+4)(w)(w-2)$$

$$8w+32 = w(w^2+2w-8)$$

$$8w+32 = w^3+2w^2-8w$$

$$0 = w^3+2w^2-16w-32$$

$$\rightarrow 0 = w^3+2w^2-16w-32$$

$$0 = w^2(w+2)-16(w+2)$$

$$= (w+2)(w^2-16)$$

$$0 = (w+2)(w-4)(w+4)$$

$$w = -2 \quad w = 4 \quad w = -4$$

reject no neg width

$$\text{width} = 4 \text{ cm}$$

$$\text{length} = 4 + 4 = 8 \text{ cm}$$

$$\text{height} = 4 - 2 = 2 \text{ cm}$$

$$4 \text{ cm} \times 8 \text{ cm} \times 2 \text{ cm}$$

HW: pg 149 #10, 14, 15, 16,
chapter review